

Donner les primitives des fonctions suivantes :

1)  $f(x) = 5x^2 - 6x + 7$

$F(x) = \dots$

2)  $f(x) = \cos(5x+6)$

$F(x) = \dots$

3)  $f(x) = \frac{1}{x^2} + \frac{1}{\sqrt{x}}$

$F(x) = \dots$

4)  $f(x) = \frac{5}{x} + \frac{1}{x^3}$

$F(x) = \dots$

5)  $f(x) = \frac{6x+7}{(3x^2+7x+4)^8}$

$F(x) = \dots$

6)  $f(x) = \frac{\cos(\pi x+4)}{\sin(\pi x+4)}$

$F(x) = \dots$

7)  $f(x) = 2(2x-9)^{14}$

$F(x) = \dots$

8)  $f(x) = \frac{x+1}{\sqrt{x^2+2x+9}}$

$F(x) = \dots$

9)  $f(x) = (9x^2 + 6)(x^3 + 2x - 4)^5$

$F(x) = \dots$

10)  $f(x) = \frac{5}{x} (\ln(\pi x))^3$

$F(x) = \dots$

Réponses :

1)  $f(x) = 5x^2 - 6x + 7$

$F(x) = \frac{5x^3}{3} - 6\frac{x^2}{2} + 7x + c = \frac{5x^3}{3} - 3x^2 + 7x + c$

2)  $f(x) = \cos(5x+6)$

$F(x) = \frac{\sin(\pi(5x+6))}{5} + c$

3)  $f(x) = \frac{1}{x^2} + \frac{1}{\sqrt{x}}$

$F(x) = \frac{-1}{x} + 2\sqrt{x} + c$

4)  $f(x) = \frac{5}{x} + \frac{1}{x^3}$

$F(x) = 5 \ln(x) + \frac{-1}{2x^2} + c$

5)  $f(x) = \frac{6x+7}{(3x^2+7x+4)^8}$

$F(x) = \frac{-1}{7(3x^2+7x+4)^7} + c$

6)  $f(x) = \frac{\cos(\pi x+4)}{\sin(\pi x+4)}$

$F(x) = \ln(\sin(\pi x+4)) + c$

7)  $f(x) = 2(2x-9)^{14}$

$F(x) = \frac{(2x-9)^{15}}{15} + c$

8)  $f(x) = \frac{x+1}{\sqrt{x^2+2x+9}}$

$F(x) = \frac{1}{2} 2\sqrt{x^2+2x+9} + c = \sqrt{x^2+2x+9} + c$

9)  $f(x) = (9x^2 + 6)(x^3 + 2x - 4)^5$

$F(x) = 3 \times \frac{(x^3+2x-4)^6}{6} + c = \frac{(x^3+2x-4)^6}{2} + c$

10)  $f(x) = \frac{5}{x} (\ln(\pi x))^3$

$F(x) = 5 \times \frac{(\ln(\pi x))^4}{4} + c$